

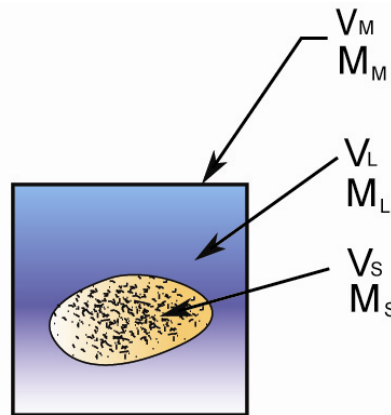
## **APPENDIX C**

THE DETERMINATION OF SLURRY DENSITY BASED ON THE VOLUME AND  
WEIGHT CONCENTRATION OF THE SOLID PARTICLES

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### THE DETERMINATION OF SLURRY DENSITY BASED ON THE VOLUME AND WEIGHT CONCENTRATION OF THE SOLID PARTICLES

This section explains how the specific gravity of a slurry ( $SG_M$ ) is related to the solid's particle weight and volume concentration.



*Figure C-1 Variables related to the calculation of the specific gravity of a slurry.*

#### Definitions

$V_M$  : volume the slurry mixture

$M_M$  : mass of the slurry mixture

$V_L$  : volume of the liquid portion of the mixture

$M_L$  : mass of the liquid portion of the mixture

$V_S$  : volume of the solid portion of the mixture

$M_S$  : mass of the solid portion of the mixture

$C_V$  : concentration by volume of the solid particles in the mixture or the **ratio** of the volume of the solids to the total mixture volume

$C_W$  : concentration by weight of the solid particles in the mixture or the **ratio** of the weight of the solids to the total mixture weight

$SG_S$  : specific gravity of the solids portion of the mixture

$SG_L$  : specific gravity of the liquid portion of the mixture

$SG_M$  : specific gravity of the mixture

$\rho_S$  : specific gravity of the solids portion of the mixture

$\rho_L$  : specific gravity of the liquid portion of the mixture

$\rho_M$  : specific gravity of the mixture

$\rho_{WA}$  : specific gravity of water at standard conditions

$M$  : mass flow rate

$q$  : volumetric flow rate

The mass of the solid particles ( $M_S$ ) is:

$$M_s = \rho_s V_s$$

and the solids density  $\rho_s$  can be expressed as a specific gravity. Specific gravity is a ratio of the density of the substance to the density of water at standard conditions  $\rho_{wa}$  :

$$\rho_s = SG_s \rho_{wa}$$

By definition  $C_w = M_s/M_M$

The volume of the mixture can be expressed as the sum of the solids volume and the carrying liquid volume:

$$V_T = \frac{C_w M_M}{\rho_s} + \frac{(1 - C_w) M_M}{\rho_L}$$

If we divide both sides of the equation by  $M_M$  we obtain:

$$\rho_M = \frac{1}{\frac{C_w}{\rho_s} + \frac{(1 - C_w)}{\rho_L}} \quad [\text{C-1}]$$

It is often easier to use the specific gravity (SG) of the substance instead of the density. Since  $\rho_s = SG_s \times \rho_{wa}$ ,  $\rho_M = SG_M \times \rho_{wa}$  and  $\rho_L = SG_L \times \rho_{wa}$  then

$$SG_M = \frac{1}{\frac{C_w}{SG_s} + \frac{(1 - C_w)}{SG_L}}$$

Similarly the weight of the mixture can be expressed as the sum of the solids weight and the carrying liquid weight:

$$M_M = C_v V_M \rho_s + (1 - C_v) V_M \rho_L$$

If we divide both sides of the equation by  $V_M$  we obtain:

$$\rho_M = C_v (\rho_s - \rho_L) + \rho_L \quad [\text{C-2}]$$

and expressed in terms of specific gravity:

$$SG_M = C_v (SG_s - SG_L) + SG_L$$

We can establish a relationship between  $C_V$  and  $C_W$  without using the specific gravity of the mixture  $SG_M$ . Notice that the right hand sides of equations C-1 and C-2 are equal, therefore:

$$C_V(\rho_S - \rho_L) + \rho_L = \frac{1}{\frac{C_W}{\rho_S} + \frac{(1-C_W)}{\rho_L}}$$

and expressed in terms of specific gravity and If the liquid is water with  $\rho_L/\rho_{WA} = 1$  then the above simplifies to:

$$C_V(SG_S - 1) + 1 = \frac{1}{\frac{C_W}{SG_S} + \frac{(1-C_W)}{1}}$$

$$C_V = \left( \frac{\frac{1}{\frac{C_W}{SG_S} + \frac{(1-C_W)}{1}} - 1}{(SG_S - 1)} \right)$$

$$C_V = \left( \frac{1}{C_W \left( \frac{1}{SG_S} - 1 \right) + 1} - 1 \right) \times \frac{1}{(SG_S - 1)}$$

[C-3]

By definition  $C_V = V_S/V_M$  and  $V_S = C_W \times M_M / \rho_S$

Therefore by substitution

$$C_V = \frac{C_W \rho_M}{\rho_S} = \frac{C_W SG_M}{SG_S}$$

or

$$SG_M = \frac{C_V SG_S}{C_W}$$

[C-4]

which means that there is a direct relationship between the specific gravity of the mixture  $SG_M$  and  $C_V$  and  $C_W$  if you know the density of the solids.

Usually the concentration by volume ( $C_V$ ), the concentration by weight ( $C_W$ ) and the specific gravity ( $SG_S$ ) of the solid particles will be given or known for a particular slurry. This is enough information to calculate the specific gravity of the slurry ( $SG_M$ ) using equation [C-3].

Often the purpose of the slurry mixture is to pump solid particles in a fluid form to a discharge point at a distance. In that case, we are mainly interested in the amount of tons per hour of solids that are transported.

The mass flow rate is given by:

$$M = \rho_s C_V q = SG_S \rho_{WA} C_V q$$

The density of water at standard condition is  $62.34 \text{ lbm/ft}^3$  using the appropriate units to obtain Imperial tons per hour (2000 lb/h):

$$M \left( \frac{\text{ton}}{\text{h}} \right) = SG_S \times \frac{62.34 \text{ lbm}}{\text{ft}^3} \times C_V \times q \left( \frac{\text{USgals.}}{\text{min}} \right) \times \frac{60 \text{ min}}{\text{h}} \times \left( \frac{\text{ft}^3}{7.48 \text{ USgals.}} \right) \times \frac{\text{ton}}{2000 \text{ lbm}}$$

After simplification, the mass flow rate is:

$$M \left( \frac{\text{ton}}{\text{h}} \right) = 0.25 SG_S C_V q \left( \frac{\text{USgals.}}{\text{min}} \right)$$

[C-5]